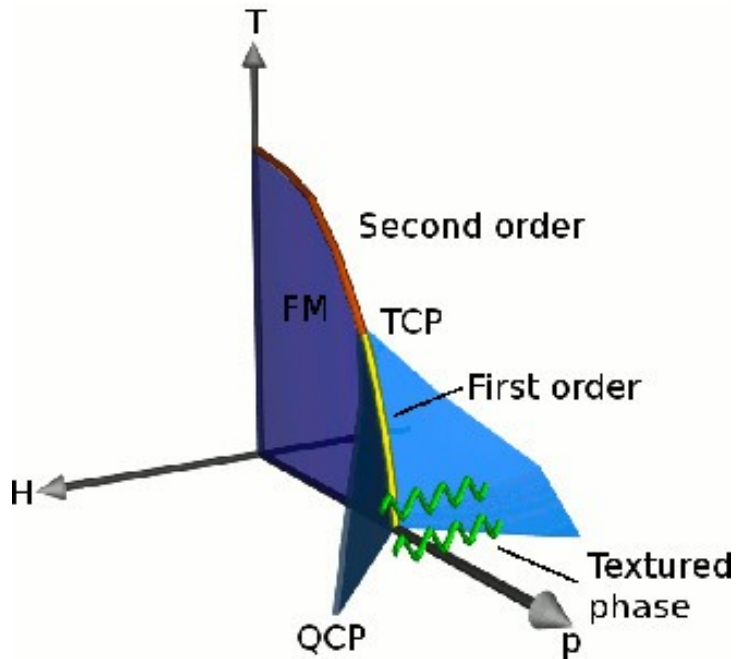


# A multi-particle Cooper pair?

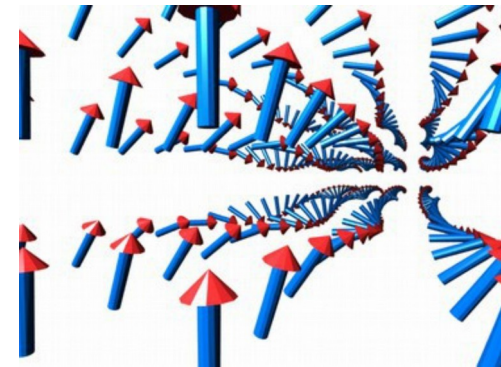
Gareth Conduit

TCM Group, Department of Physics

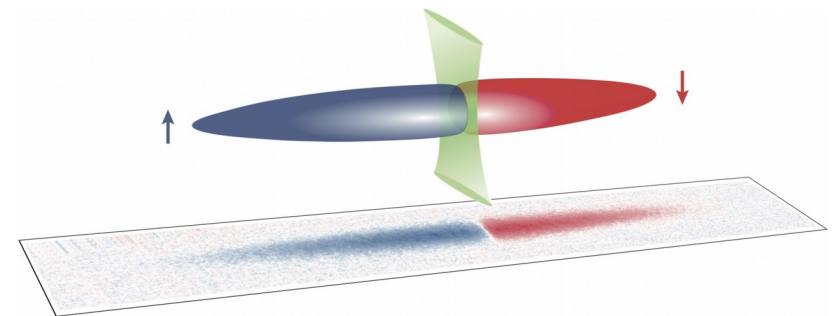


Fluctuation corrections drive exotic quantum phases

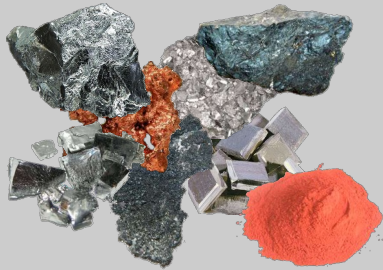
CeFePO (2012)



Cold atom gas (2016)



## Composition



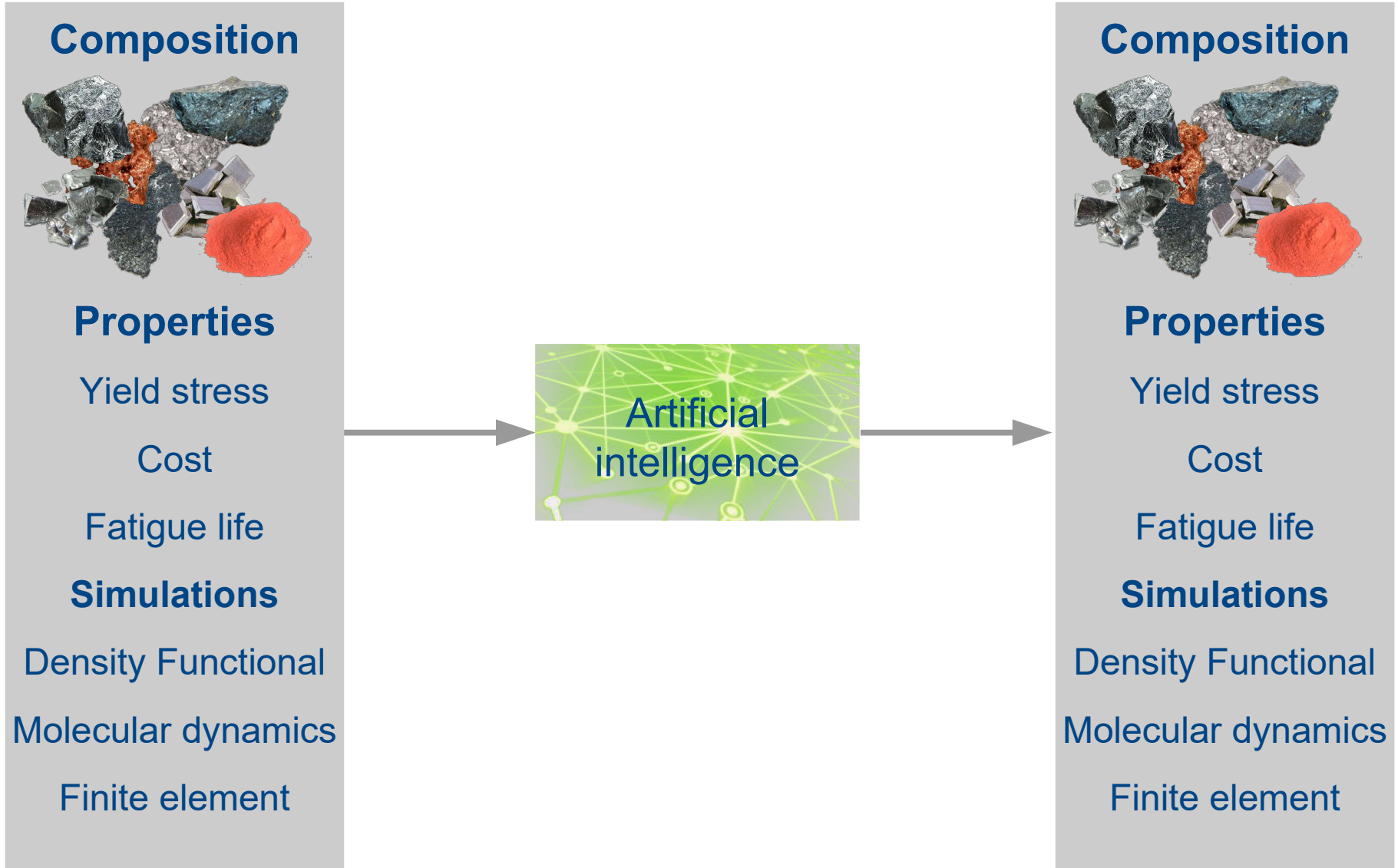
Artificial  
intelligence

## Properties

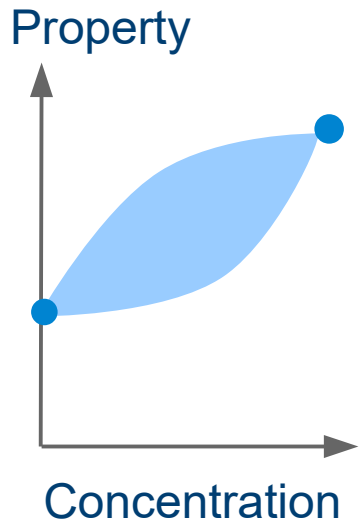
Yield stress

Cost

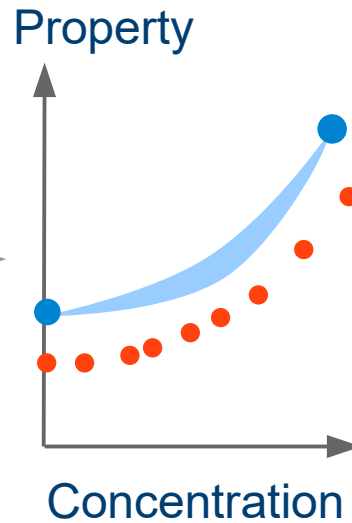
Fatigue life



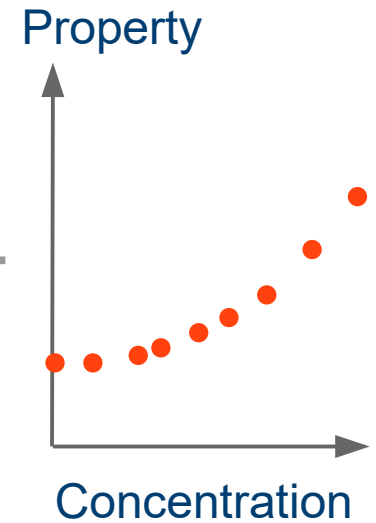
Experiment



Combined



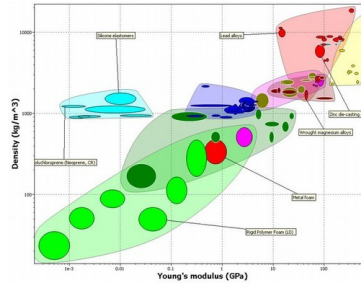
Simulation



*Experimental*  
Alloys for turbine  
blades



*Experimental*  
Materials databases



*Structural and  
experimental*  
Drug discovery



e-Therapeutics plc  
systems biology drug discovery

*DFT and experimental*  
Battery design

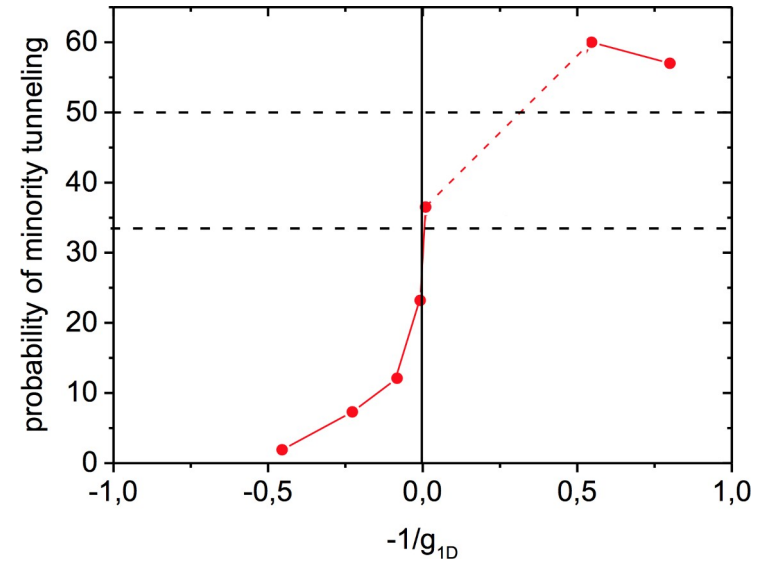
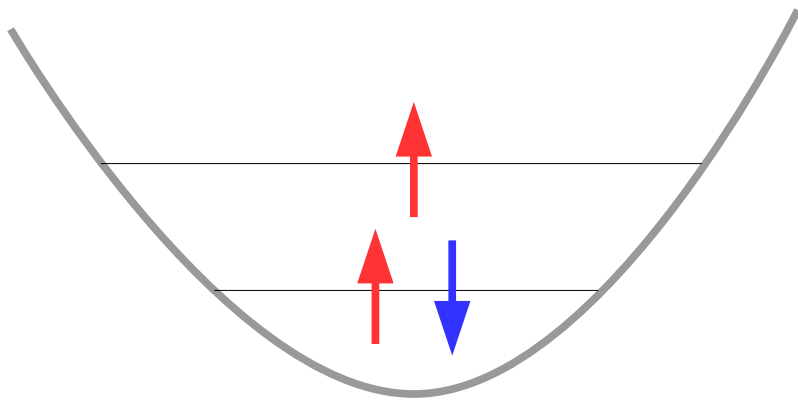


*DFT and experimental*  
Lubricants



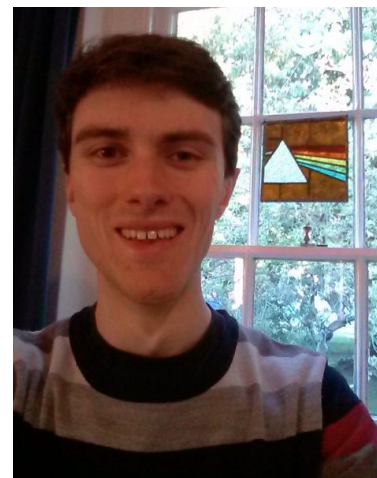
*Quantum mechanics*  
*and experimental*  
Thermometer



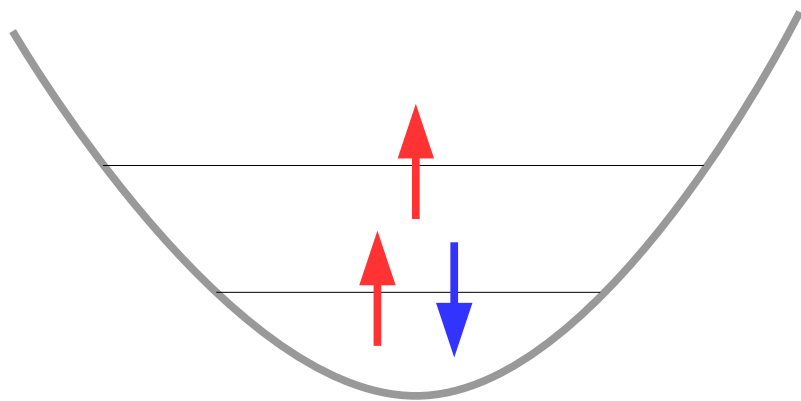


Characterization of the few-many particle crossover and ferromagnetism

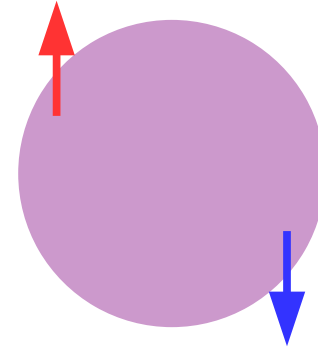




Thomas Whitehead

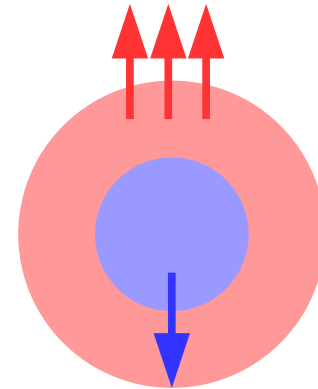


Standard superconductor



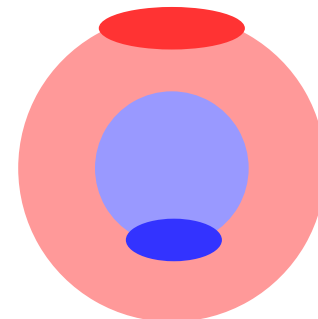
Few-body instability

Analytical  
Numerical

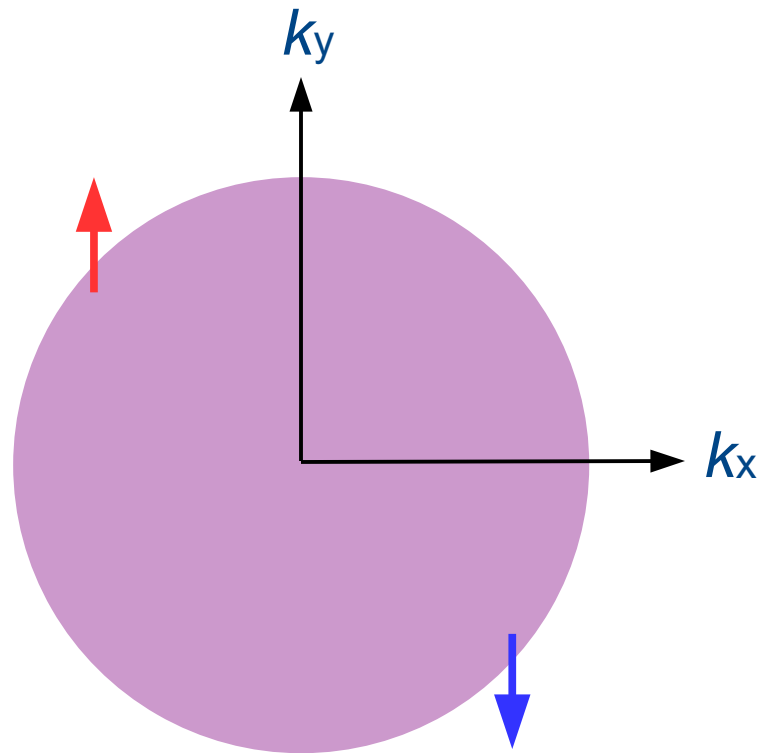


Many-body problem

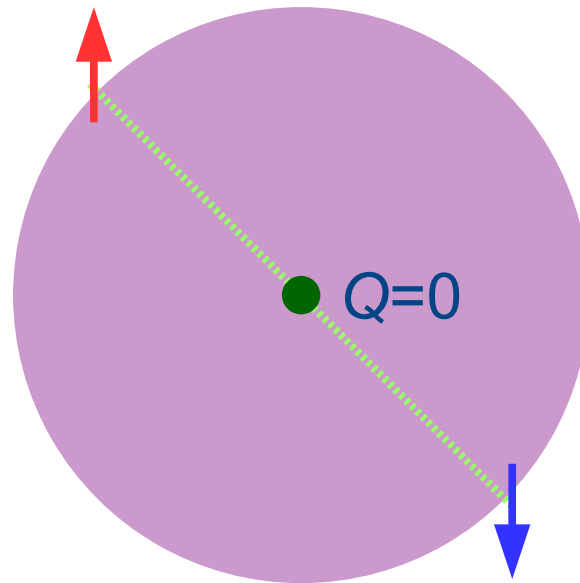
Analytical  
Numerical



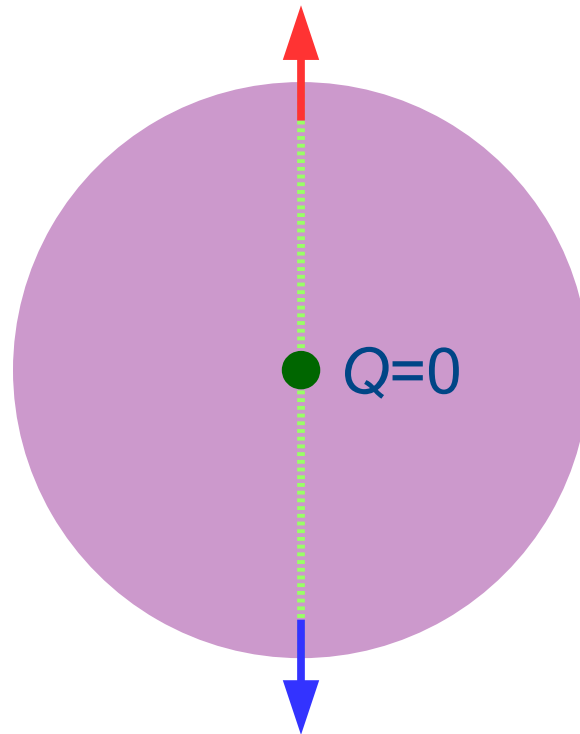
# Cooper pair



# Cooper pair

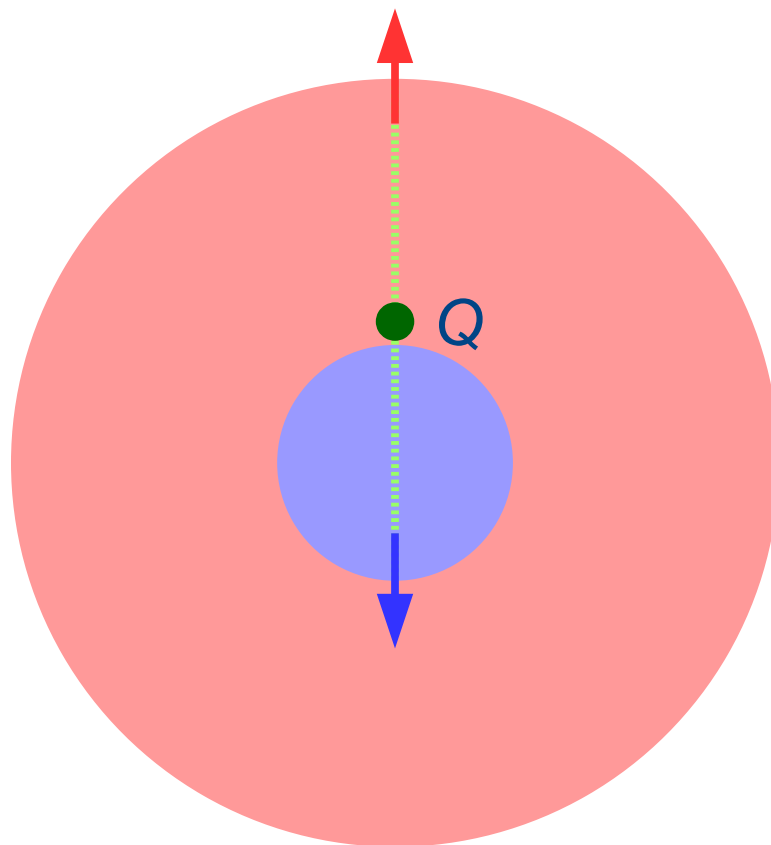


# Cooper pair

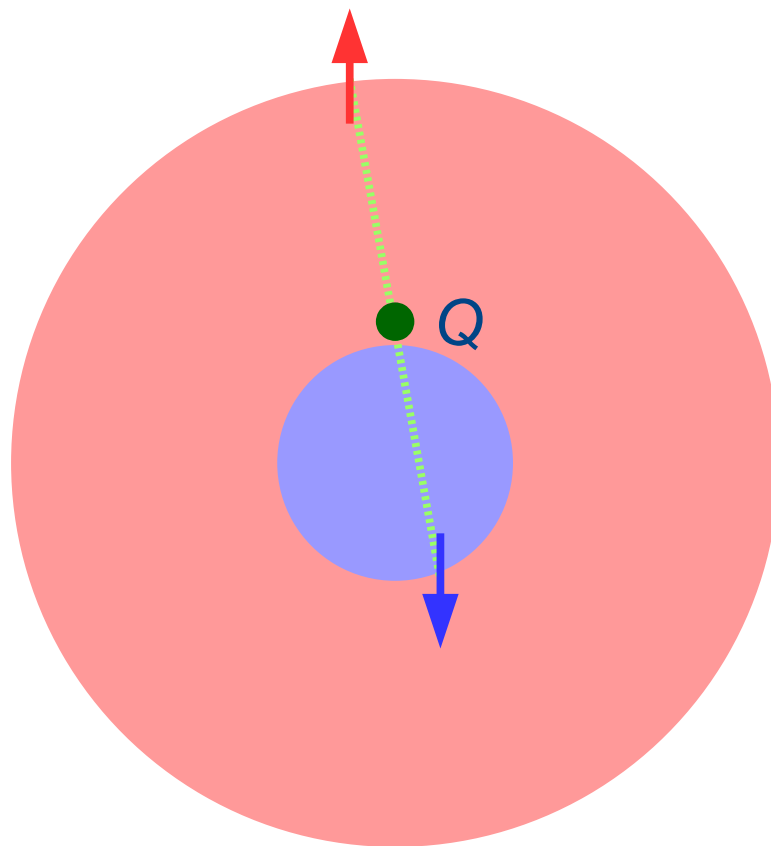


Binding energy of a Cooper pair  $E = 2 \omega_D \exp\left(-\frac{2}{g v}\right)$

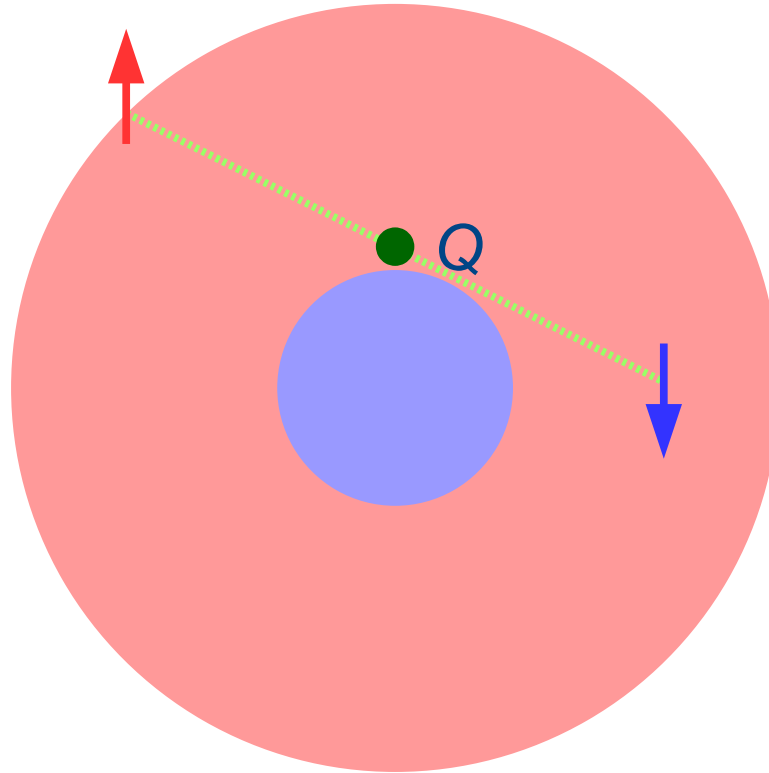
# Cooper pair in imbalanced Fermi sea



# Cooper pair in imbalanced Fermi sea

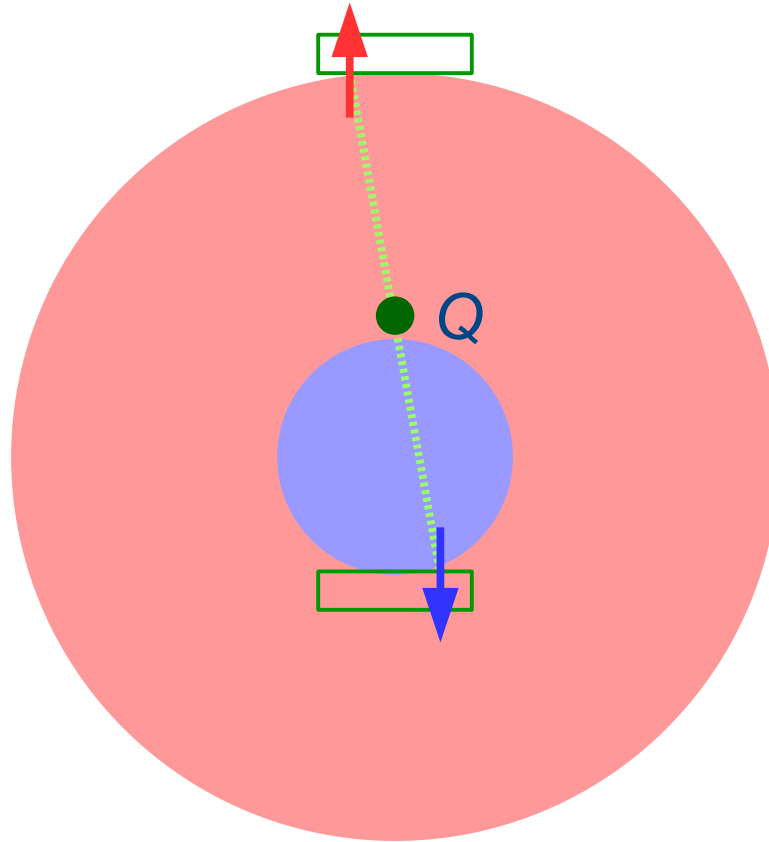


# Cooper pair in imbalanced Fermi sea

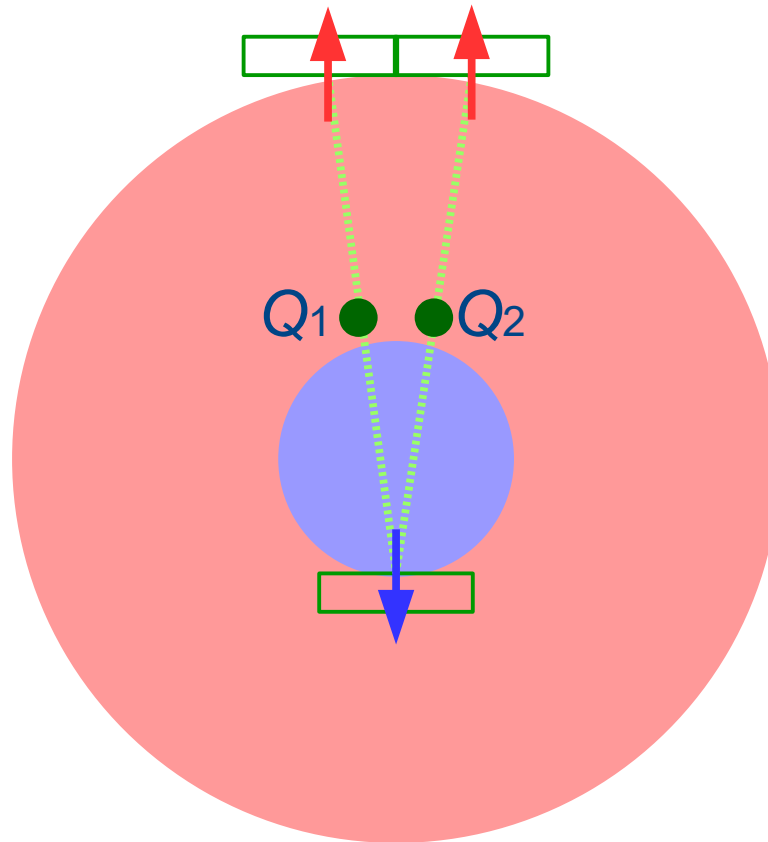




# Region of correlation



# Multiple majority spins in the Cooper particle



# Energy

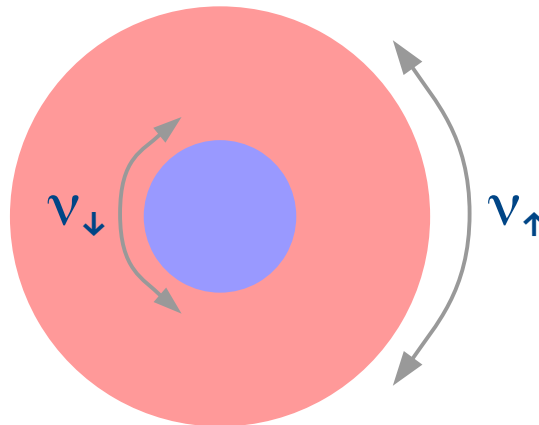
Binding energy of a Cooper particle

$$E = (N_{\uparrow} + N_{\downarrow}) \omega_D \exp\left(-\frac{(N_{\uparrow} + N_{\downarrow}) \xi' N_c}{g N_{\uparrow} N_{\downarrow}}\right)$$

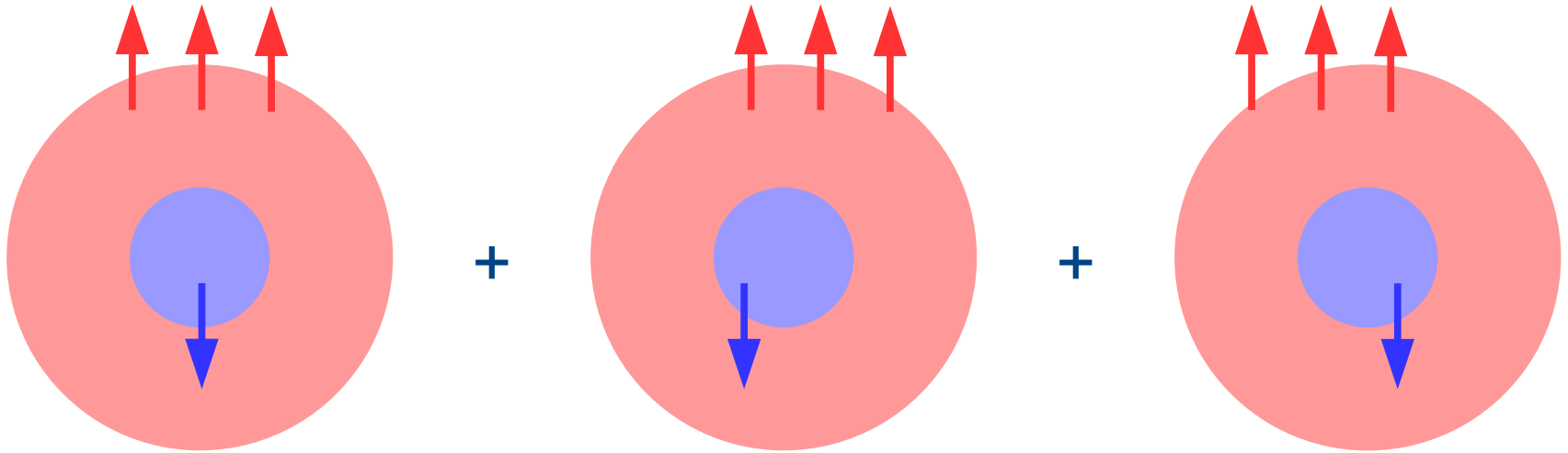
$$E = 2 \omega_D \exp\left(-\frac{2 \xi'}{g v}\right)$$

Optimal number of up and down spin electrons in a Cooper particle is

$$\frac{N_{\uparrow}}{N_{\downarrow}} = \frac{v_{\uparrow}}{v_{\downarrow}}$$



# Many-body superconductor



Superconducting transition temperature (even  $N_{\uparrow}+N_{\downarrow}$ )

$$T_c = \omega_D \exp\left(-\frac{(N_{\uparrow}+N_{\downarrow})\xi' N_c}{2gN_{\uparrow}N_{\downarrow} v_c}\right)$$

Peak transition temperature is at the number ratio

$$\frac{N_{\uparrow}}{N_{\downarrow}} = \frac{v_{\uparrow}}{v_{\downarrow}}$$

# Summary of many-particle Cooper instability

Optimal number of up and down spin electrons in a superconducting state is the ratio of the density of states

## Future consequences

- Competition with the FFLO state

- Experimental observation

- Spin orbit and mass imbalanced systems

- Number fluctuations in balanced superconductor